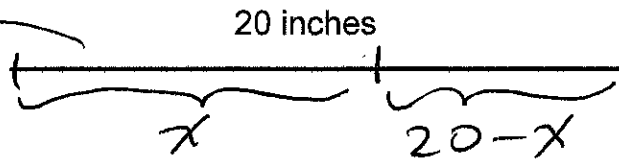
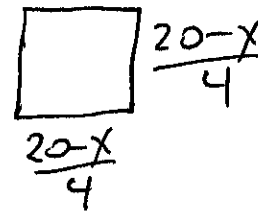
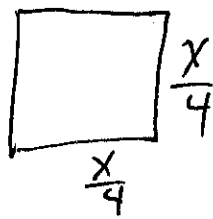


Ex: A 20 inch wire is cut into two pieces, where each piece is used to form a square.



- 1) Express the total area as a function of the length of one of the pieces.
- 2) Find the length of each piece that would maximize the area.

If we bend
length of x
into a square,
then each
side will be $\frac{x}{4}$



$$\begin{aligned}
 1) \quad A &= \frac{x}{4} \left(\frac{x}{4} \right) + \frac{20-x}{4} \frac{20-x}{4} \\
 &= \frac{1}{16} x^2 + \frac{1}{16} (20-x)(20-x) \\
 &= \frac{1}{16} x^2 + \frac{1}{16} (400 - 40x + x^2) \\
 &= \frac{1}{16} x^2 + \frac{400}{16} - \frac{40}{16} x + \frac{x^2}{16} \\
 &= \frac{1}{16} (2x^2 - 40x + 400) \\
 &= \frac{1}{8} (x^2 - 20x + 200)
 \end{aligned}$$

$$2) \quad x = \frac{-b}{2a} = \frac{-(-20)}{2(1)} = 10$$

Both pieces would be 10 inches.

Ex: Graph

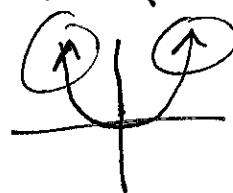
$$P(x) = \underbrace{x^4 - 2x^3 + 8x - 16}$$

$$= x^3(x-2) + 8(x-2)$$

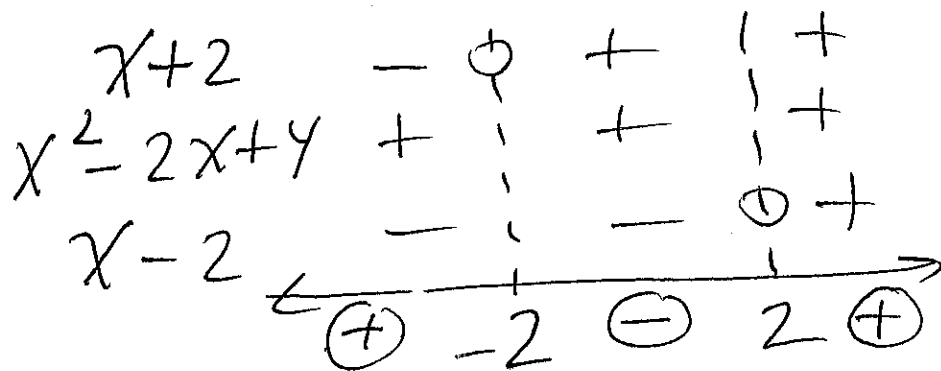
$$= (x^3 + 8)(x-2)$$

$$= (x+2)(x^2 - 2x + 4)(x-2)$$

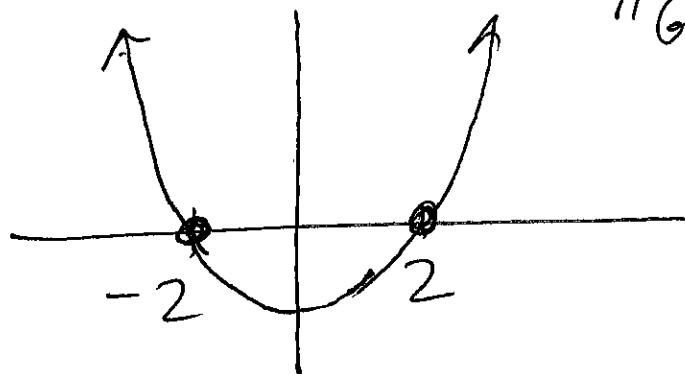
1) $x\text{-int} = -2$ } No $x\text{-int}$ from this factor } $x\text{-int} = 2$

2) leading term = x^4 

3) sign chart



4) Graph



"Graph given info found above"